Synthesis, Crystal Structure, and Thermal Behavior of the Rare Earth Sulfates $(H_5O_2)M(SO_4)_2$ $(M = Ho, Er, Y)$

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The compounds $(H_5O_2)M(SO_4)_2$ (M = Ho, Er, Y) were obtained from the metal oxides M_2O_3
1 = Ho, Er, Y) using diluted sulfuric acid (80%). The crystal structure of the isotynic ($M = H$ o, Er, Y) using diluted sulfuric acid (80%). The crystal structure of the isotypic
compounds has been determined from single-crystal data by direct and Fourier methods compounds has been determined from single-crystal data by direct and Fourier methods [tetragonal, *IA*₁/*amd* (No. 141); (H₅O₂)Ho(SO₄)₂, *a* = 6.9140(5) Å, *c* = 17.246(2) Å, *R* = 0.013; (H₅O₂)Fr(SO₄)₂, *a* = 6.8967(7) Å, *c* = 17.166(2) Å, *R* = 0.012; (H₅O₂)Y(SO₄)₂, *a* = 6.887 (H₅O₂)Er(SO₄)₂, $a = 6.8967(7)$ Å, $c = 17.166(2)$ Å, $R = 0.012$; (H₅O₂)Y(SO₄)₂, $a = 6.8875(7)$
Å $c = 17.159(2)$ Å $R = 0.0161$ The characteristic feature of the crystal structure is a network Å, $c = 17.159(2)$ Å, $R = 0.016$]. The characteristic feature of the crystal structure is a network of edge-sharing $[MO_8]$ trigon dodecahedra and $[SO_4]$ tetrahedra providing channels along [111] which are occupied by disordered H_5O_2 ⁺ ions. In situ X-ray powder investigations exhibit that the compounds are also formed as intermediate phases during the reaction of the hydrogen sulfates $M(HSO₄)₃$ (M = Ho, Er, Y) with water. According to DSC measurements and temperature-dependent powder diffraction studies, the thermal decomposition of the title compounds follows a two-step mechanism. Around 150 °C, two molecules of water are driven off, yielding M(HSO₄)(SO₄) (M = Ho, Er, Y), and finally, at 320 °C, H₂SO₄ (H₂O $+$ SO₃) is released to give the anhydrous sulfates $M_2(SO_4)_3$.

Introduction

Sulfates of the rare earth elements and their derivatives have rarely been investigated. Reliable structural data are available only for a few compounds, namely hydrates such as $Pr(SO_4)_2$ ·8H₂O and "ternary" sulfates such as $\text{NaNd}(\text{SO}_4)_2$.^{1–3} Recently, the hydrogen sulfates of some rare earth elements, $M(HSO₄)₃$ (M = La, Ce-Er) were synthesized by the reaction of lanthanide oxides with concentrated sulfuric acid at elevated temperatures. $4-5$ Reduction of the acid concentration and the reaction temperature then led to the oxonium rare earth sulfate hydrates $(H₅O₂)M(SO₄)₂$. There is one compound of the same composition described in the literature ($M = Ce$),⁶ but its structure is found to be completely different. Two further oxonium compounds, $H_3OLa(SO_4)_2 \cdot 3H_2O$ and $(H_3O)_3Nd(SO_4)_3 \cdot H_2O$, are available under similar conditions and will be discussed elsewhere.7 In this study, the crystal structure of the title compounds and their thermal behavior will be presented. Furthermore, it is shown that the compounds are intermediate products during the hydration of the respective hydrogen sulfates.

Experimental Section

Single crystals of the compounds $(H_5O_2)M(SO_4)_2$ (M = Ho, Er, Y) were grown as follows: 1 g of the oxides Ho_2O_3 (99.99%,

Aldrich), Y_2O_3 (99.99%, Aldrich), and Er_2O_3 (99.99%, Heraeus), respectively, was dissolved in 30 mL of hot (100 °C) sulfuric acid (Merck p.a, concentrated 80% H₂SO₄). After cooling, the solutions were allowed to stand in closed vessels for 5 days. During this time, crystals of orange-yellow $(H_5O_2)Ho(SO_4)_2$, pink $(H_5O_2)Er(SO_4)_2$, and colorless $(H_5O_2)Y(SO_4)_2$ grew as elongated octahedra up to a size of 5 mm. The crystals were washed with absolute tetrahydrofuran free of their mother liquor. Due to their moisture sensitivity, the crystals must be handled in an argon filled glovebox. Small crystals of about 0.1 mm in diameter were prepared in glass capillaries for X-ray data collection. The scattering intensities were collected with an imaging plate diffractometer (STOE&CIE). The systematic absences in the collected data set led to the tetragonal space group *I*41/*amd* (No. 141) for the three compounds. Structure solution and refinement were carried out using the programs SHELXS86 and SHELXL93.8 A numerical absorption correction was applied after optimization of the crystal shape (programs X-RED and X-SHAPE9). The data collection parameters and the determined crystallographic data are given in Tables $1 - 3$.

DSC/TG investigations were performed using a STA 409 thermal analyzer (NETZSCH). For that purpose, about 10 mg of the substances was placed in corundum containers and heated at a constant rate of 10 K/min under flowing argon. The thermal decomposition was followed from 30 °C up to 500 °C. For the DSC data, a baseline correction was applied. Characteristical points such as the start and end temperatures

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Table 1. Data Collection Parameters and Crystal Data for $(H_5O_2)M(SO_4)_2$; $M = Ho (1)$, Er (2), Y (3)

	1	$\boldsymbol{2}$	3		
lattice parameters $a = 6.9140(5)$		$a = 6.8967(7)$	$a = 6.8875(7)$		
(A)	$c = 17.246(2)$	$c = 17.166(2)$	$c = 17.159(2)$		
molar volume	124.1	122.9	122.6		
(cm ³ /mol)					
no. of formula units, Z		4			
crystal system		tetragonal			
space group	$I4_1$ /amd (No. 141)				
diffractometer	STOE IPDS				
radiation		Mo Kα (graphite monochromator,			
	$\lambda = 0.7107$ Å)				
temperature $(^{\circ}C)$		20			
data range	$6^\circ \leq 2\theta \leq 48^\circ$	$6^{\circ} < 2\theta < 48^{\circ}$	$6^\circ \leq 2\theta \leq 48^\circ$		
index range	$-9 \leq h \leq 9$	$-9 \leq h \leq 9$	$-7 \leq h \leq 7$		
	$-8 \leq k \leq 9$	$-9 \leq k \leq 9$	$-7 \leq k \leq 7$		
	$-21 \le l \le 22$	$-20 \le l \le 22$	$-19 \le l \le 19$		
rotation angle	$0^{\circ} < \varphi < 200^{\circ}$;	$0^{\circ} < \varphi < 200^{\circ}$;	$0^{\circ} < \varphi < 200^{\circ}$;		
range;	$\Delta\varphi=2^{\circ}$	$\Delta\varphi=1.5^{\circ}$	$\Delta\varphi=2^{\circ}$		
φ -increment					
no. of images	100	133	100		
exposure time	2.5 min	4.0 min	4.0 min		
detector distance	60 mm	60 mm	80 mm		
data corrections		polarization/Lorentz			
absorption		numerical, after crystal shape optimization ⁹			
corrections					
μ (cm ⁻¹)	101.4	108.2	97.3		
no. of collected	2364	2387	2374		
reflections					
	189	188	190		
no. of unique reflections					
no. of reflections	188				
		186	176		
with $I_0 > 2\sigma(I)$	0.0320	0.0301			
$R_{\rm int}$ structure			0.0464		
	SHELXS-86 and SHELXL-938				
determination					
scattering factors		International Tables, Vol. C ¹⁷			
goodness of fit	1.063	1.042	1.088		
R_1 ; $wR_2 I_0 > 2\sigma(I)$	0.0135:	0.0122:	0.0156		
	0.0351	0.0353	0.0360		
R_1 ; wR_2	0.0137:	0.0126;	0.0166:		
(all data)	0.0352	0.0356	0.0365		

of the thermal effects were taken from the differentiated DSC curve following common procedures.10

Temperature-dependent powder diffraction data were collected using a powder diffractometer (STOE&CIE) equipped with a position sensitive detector and a graphite furnace. The fine powdered samples were prepared in silica capillaries (i.d. $= 0.3$ mm) and sealed with grease (APIEZON L) for protection against moisture. Data were collected in Debye-Scherrer geometry in the range of $2\theta = 7^{\circ}-60^{\circ}$ at temperatures of 30, 60, 120, 180, 240, 300, and 360 °C, respectively. After each heating period, the system was allowed to equilibrate for 30 min. The data were processed by applying smoothing and background corrections using the program package VISUAL X-POW11 (STOE&CIE). The same program allowed for lattice parameter refinements based on least-squares procedures.

The reaction of hydrogen sulfates $M(HSO_4)_3$ (M = Ho, Er, Y), which were synthesized following the route given in ref 4, with water (moisture), was investigated on a *θ*/*θ* powder diffractometer (STOE&CIE) equipped with a HDK 2.4 reaction chamber (BÜHLER). Powder samples were placed on a small silver plate in the chamber, which was first purged with dry N_2 . After collection of the first diffractogram, a small window of the chamber was opened to allow moisture to enter. Eight diagrams were continuously collected in the range $2\theta = 7^{\circ}$ 60°. The data were handled using the program VISUAL X-POW.

Figure 1. Crystal structure for $(H_5O_2)H_0(SO_4)_2$ viewed along [110]; $[SO_4]^{2-}$ groups are drawn as polyhedra; Ho-O bonds are black; both orientations of the $H_5O_2^+$ ion are shown.

Figure 2. The $H_5O_2^+$ ion in $(H_5O_2)H_0(SO_4)_2$: The O3 position is only half-occupied, the resulting orientations of the ion are shown as dark gray and light gray O3 atoms and O3-H1 bonds, respectively; hydrogen bridging is indicated by broken lines, distances are given in Å.

Results and Discussion

Crystal Structure.¹⁸ The compounds (H₅O₂)M(SO₄)₂ $(M = Ho, Er, Y)$ crystallize in a hitherto unknown structure type with the tetragonal space group *I*41/*amd*. The crystallographic data are given in Tables 1 and 2. The structure consists of $[MO_8]$ polyhedra which can be grasped as trigon dodecahedra. These are connected to six sulfate groups in two different ways: Along [001], two [SO4] groups are attached via two common edges, and in the (001) plane, linkage occurs to four additional [SO4] groups via vertexes (Figure 1). Thereby each sulfate group belongs to three M^{3+} ions and the connectivity can be written as $M(SO_4)_{6/3} = M(SO_4)_2$ following Niggli's notation. ${\rm H_5O_2}^+$ ions are incorporated in the three-dimensional framework of these polyhedra. This leads to an alternating occupancy of dodecahedral voids with M^{3+} and $H_5O_2^+$, respectively, along [110] (Figure 1). The H_5O_2 ⁺ ions are disordered in the way depicted in Figure 2. Free refinement of the site occupation factor of the oxygen atom O3 clearly revealed an occupancy of 0.5 of this position (16h, Table 2).

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Table 2. Positional Parameters and Equivalent Isotropic Displacement Parameters for $(H_5O_2)M(SO_4)_2$ **(M = Ho in italics,** $M = Y$ **bold type)**

atom	site	x/a	y/b	Z/c	U_{eq} \cdot 10 ⁻¹ , pm ^{2 a}
Er	4a	$\mathbf{0}$	3/4	1/8	10.5(2)
H ₀		0	3/4	1/8	10.9(2)
Y		0	3/4	1/8	13.4(2)
S	8e	$\bf{0}$	1/4	0.9482(1)	12.7(4)
		0	1/4	0.94814(9)	12.8(3)
		0	1/4	0.94830(5)	14.7(2)
01	16h	0	0.0823(5)	0.7522(2)	22.9(4)
		0	0.0832(5)	0.7516(1)	20.8(7)
		0	0.0824(3)	0.7518(1)	22.9(4)
O ₂	16h	$\mathbf{0}$	0.5780(5)	0.8992(2)	24.5(4)
		0	0.5781(5)	0.8991(2)	22.1(7)
		0	0.5779(3)	0.8994(1)	24.5(4)
O3 ^b	16h	0	0.1551(16)	0.4402(6)	51.2(24)
		0	0.1584(16)	0.4406(6)	47.9(24)
		0	0.1569(9)	0.4400(3)	54.2(16)
H1	4 _b	0	1/4	3/8	$108(88)^{c}$
		0	1/4	3/8	$53(48)^c$
		0	1/4	3/8	$99(39)^{c}$
$H2^b$	32i	0.624(19)	0.715(18)	0.977(7)	$150(91)^{c}$
		0.64(2)	0.70(4)	0.970(8)	$147(87)$ c
		0.608(7)	0.684(8)	0.963(3)	$57(20)^c$

a $U_{eq} = 1/3[U_{11} + U_{22} + U_{33}]$.¹² *b* Site half-occupied. *c* Isotropic displacement parameter.

Table 3. Selected Internuclear Distances [Å] and Angles $[deg]$ for the Compounds $(H_5O_2)M(SO_4)_2$ $(M = Er, Ho, Y)$

	$M = Er$	$M = Ho$	$M = Y$		
$M - O2$ (4 \times)	2.300(3)	2.306(3)	2.297(2)		
$M-O1(4\times)$	2.404(3)	2.420(3)	2.408(2)		
$S - O2(2x)$	1.454(3)	1.458(3)	1.452(2)		
$S - O1(2x)$	1.482(3)	1.477(3)	1.476(2)		
$O1 - S - O1$	102.6(3)	102.6(3)	102.9(1)		
$01 - S - 02(4)$	111.20(8)	111.24(9)	111.09(6)		
$O2-S-O2$	109.3(3)	109.1(3)	109.4(1)		
Hydrogen Bonding					
$O3-H2$	1.13	1.17	0.85		
$O3 - H1$	1.29	1.30	1.287		
$H2-O1$	1.51	1.45	1.74		
$O(3 - O1)$	2.608(5)	2.610(4)	2.603(3)		
$O3 - O3$	2.475(3)	2.436(3)	2.410(3)		
$O3 - H2 - O1$	162.9	172.8	174.8		
$O3 - H1 - O3$	137.3	139.6	138.8		

Furthermore, complete occupation would lead to O3- O3 distances of 1.3 Å. Two orientations of the $H_5O_2^+$ ion are possible, leading to short O3-O1 distances of about 2.6 Å, yielding effective hydrogen bonding between H2 and O1 (Table 3). Due to the disorder, the displacement parameters of O3 are quite large. From X-ray data, however, one cannot decide whether one deals with a dynamic process or a static order/disorder phenomenon. Another interesting feature of the $\mathrm{H_5O_2}^+$ ion is the position of the atom H1. From inspection of the difference Fourier map, the most likely location is $0.1/4$, $3/8$. As can be seen from Figures 1 and 2, respectively, this leads to a symmetric O3-H1-O3 hydrogen bond. A strong argument for such an arrangement is the short O3-O3 distance of 2.44 Å within the ion. It compares well with systems such as $H_2SO_4 \cdot 4H_2O^{13}$ (2.43) Å) or $HClO_4$ ·2 H_2O^{14} (2.42 Å), where a symmetric hydrogen bond or at least a low barrier double minimum potential has been assumed. In contrast to these

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Figure 3. Crystal structure of $(H₅O₂)H₀(SO₄)₂$ viewed along [111]: All possible O3 positions are drawn and connected to distorted tetrahedra centered by H1. These tetrahedra are localized in channels running down this direction; O3-H2 bonds are emphasized in black.

Figure 4. DSC investigation of the thermal decomposition of $(H_5O_2)Y(SO_4)_2$: The baseline-corrected DSC curve shows two endothermic effects at 163 and 342 °C. Both effects are correlated with a mass loss indicated by the TG curve.

systems, however, where the bond angle O-H-O is near 180°, the compounds under investigation show an O3-H1-O3 angle of 140° (Table 3), which indicates a nonsymmetric hydrogen bond. This, however, cannot be judged with certainty from the X-ray investigations. Assuming the given H1 and all possible O3 positions, the $H_5O_2^+$ (=H(H₂O)₄) ions can be drawn as elongated
tetrahedra. These are arranged in channels along [111] tetrahedra. These are arranged in channels along [111] with the nearest O-O distances of 2.92 Å bearing the possibility of protonic motion along this direction (Figure 3).

Thermal Behavior. By thermal treatment the compounds $(H_5O_2)M(SO_4)_2$ (M = Ho, Er, Y) decompose in a two-step mechanism that is discussed in detail for the yttrium compound in the following text. The DSC measurement (Figure 4) shows a mass loss of 10.4% in the range of $147-172$ °C and a second mass loss of 14.9% in the range of $333-352$ °C (Table 4). The first step can be assigned to the loss of two molecules of water

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Table 4. DSC Results of the Thermal Decomposition of $(H_5O_2)Y(SO_4)_2$

					mass loss	
reaction	T_{start} (°C)	T_{end} (°C)	$T_{\rm max}$ (°C)	obsd	calcd	
$(H_5O_2)Y(SO_4)_2 \longrightarrow T_{2H_2O}Y(HSO_4)(SO_4)$	147.4	172.4	163.5	10.2	11.3	
$Y(HSO_4)(SO_4)_2 \xrightarrow[1/2]{1/2} O_4 \xrightarrow[1/2]{1/2} Y_2(SO_4)_3$	333.3	351.8	341.9	14.9	15.4	
				$\Sigma = 25.1$	$\Sigma = 26.7$	

Figure 5. Temperature-dependent X-ray powder diffraction of $(H_5O_2)Y(SO_4)_2$: The diagrams 1 and 2 belong to (H_5O_2) -Y(SO4)2, diagram 3 is mainly the same, but a few peaks of $Y(HSO₄)(SO₄)$ start to occur. Up to 300 °C, the diffraction patterns $(4-6, \text{gray})$ can be assigned to $Y(\text{HSO}_4)(\text{SO}_4)$. At 360 $\rm{^{\circ}C}$, Y₂(SO₄)₃ has formed (7, light gray).

(calcd 11.3%) and the second step corresponds to the loss of 0.5 mol of sulfuric acid (calcd 15.4%). The decomposition reactions and the related data are given in Table 4.

The suggested mechanism is supported by temperature-dependent powder diffraction investigations (Figure 5). At 30 and 60 °C, the diffractograms could be indexed using simulated patterns based on singlecrystal data. The same is true for the measurement at 120 °C, although a few reflections between $2\theta = 18$ -30° remained unindexed. The unindexed reflections can be assigned to $Y(HSO₄)(SO₄)$, which begins to form at this temperature. The difference in the decomposition temperatures determined by DSC and powder diffraction can be attributed to the different measuring conditions of the two methods. At 180 °C, the diffractogram contains only reflections of Y(HSO₄)(SO₄). Indexing was possible using single-crystal data of $Er(HSO₄)(SO₄)$ which where obtained recently.⁴ Y(HSO₄)(SO₄) remains stable at 300 °C, but complete decomposition to $Y_2(SO_4)_3$

Figure 6. X-ray powder investigation of the hydration of Er- $(HSO₄)₃$ (pattern 1, black): In the first step, $(H₅O₂)Er(SO₄)₂$ formed rapidely (patterns 2 and 3, light gray). Further hydration yields $Er_2(SO_4)_3$ ·8H₂O (patterns 5 and 6, black). In diffractogram 4 (gray) $(H_5O_2)Er(SO_4)_2$ and $Er_2(SO_4)_3.8H_2O$ occur simultanuously.

is observed at 360 °C. The powder diffractogram of the latter compound could be indexed using the singlecrystal data of $Er_2(SO_4)_3$.⁴ The refined lattice parameters of all compounds are given in Table 5.

Hydration of M(HSO₄)₃ ($M = Ho$, Er, Y). The first step of the reaction of hydrogen sulfates $M(HSO₄)₃$ (M $=$ Ho, Er, Y) with H₂O leads to the title compounds $(H_5O_2)M(SO_4)_2$ (M = Ho, Er, Y) and, finally, to the formation of the octahydrates $M_2(SO_4)_3$ ^{-8H₂O. This is} shown in Figure 6 for $M = Er$. The diffraction patterns collected during the reaction could be indexed using the $\text{single-crystal data of }\text{Er}(\text{HSO}_4)_3.^4\text{Er}_2(\text{SO}_4)_3.^3\text{8H}_2\text{O}^{15}$ and $\text{(H-O_9)Fr}(\text{SO}_4)_2$. The reaction sequence is given by the $(H₅O₂)E_r(SO₄)₂$. The reaction sequence is given by the equations:

$$
Er(HSO_4)_3 + 2H_2O \rightarrow (H_5O_2)Er(SO_4)_2 + H_2SO_4
$$
 (1)

$$
2(H_5O_2)Er(SO_4)_2 + 4H_2O \rightarrow Fr_2(SO_4)_3 \cdot 8H_2O + H_2SO_4
$$
 (2)

Both reactions are typical acid/base reactions with H_2O

Table 6. X-ray Powder Diffraction Results for the Hydration of Er(HSO₄)₃

acting as the base. In reaction 1, the $\mathrm{HSO_4}^-$ ion plays the role of the acid, and in reaction 2, it is the $H_5O_2^+$ ion. It is noteworthy that no formation of $Er(HSO_4)_3$. $H₂O¹⁶$ is observed during the first reaction, and the compound $Er_2(SO_4)_3 \cdot 4H_2O^{16}$ is not observed. The conversion of Er(HSO₄)₃ seems to occur quite rapidly, while the formation of the octahydrate takes some time, as

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can be seen from the fourth diffractogram (Figure 6, Table 6), where both compounds occur together.

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⁽¹⁸⁾ Crystallographic data are available from the Fachinformationszentrum Karlsruhe, D-76344 Eggenstein-Leopoldshafen (crysdata@FIZ-Karlsruhe.de) by giving the deposition numbers CSD 408876 $(\mathrm{H}_5\mathrm{O}_2\text{-}$
Ho(SO4)2), CSD 408875 (H5O2Er(SO4)2), and CSD 408877 (H5O2Y(SO4)2, respectively.